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EXTENDED TABLES OF STIFFNESS AND CARRY-OVER FACTOR

FOR STRUCTURAL MEMBERS UNDER AXIAL LOAD

By Eugene E. Lundquist and W. D. Kroll

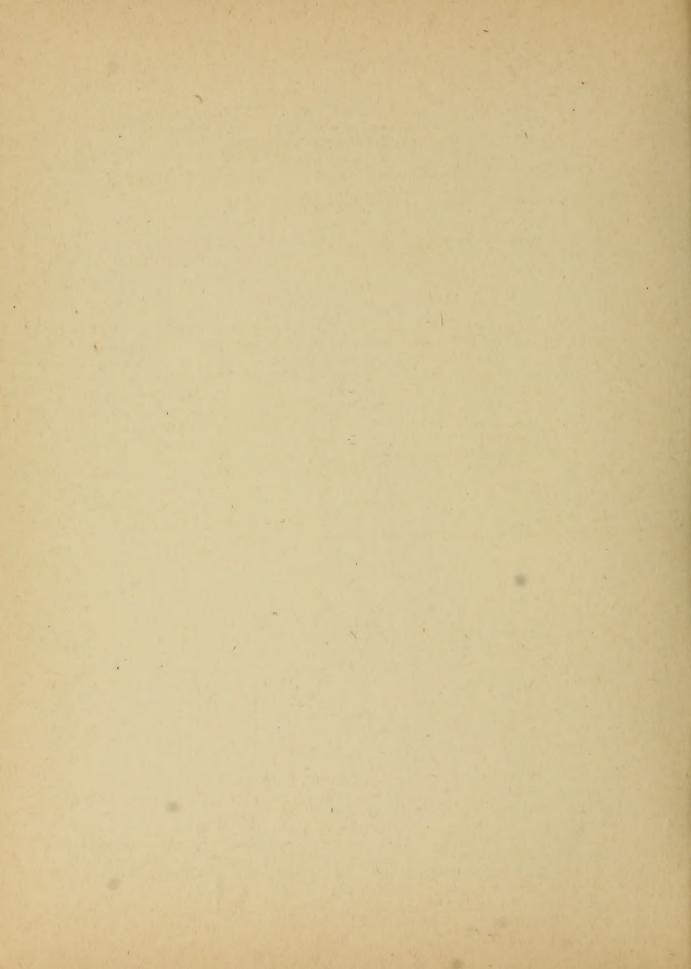
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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

ADVANCE RESTRICTED REPORT

EXTENDED TABLES OF STIFFNESS AND CARRY-OVER FACTOR

FOR STRUCTURAL MEMBERS UNDER AXIAL LOAD

By Eugene E. Lundquist and W. D. Kroll

SUMMARY

The tables of stiffness and carry-over factor that were presented in NACA Technical Note No. 652 have been extended to include the stiffness of a member with the far end subjected to a moment equal and opposite to the moment applied at the near end. These tables are of use in solving problems in the stability of structural members under axial load as well as in the usual applications of the Cross method of moment distribution when the effects of axial load in the members are considered. The values presented are for structural members in which the cross section and the axial load do not vary along the length of the member. The interval between successive values of the argument is small enough to make interpolation unnecessary in engineering calculations.

INTRODUCTION

The tables of stiffness and carry-over factor given in reference I have been found useful in the applications of moment-distribution methods to a number of structural problems. Recent studies have shown the desirability of including in these tables an additional stiffness that was not formerly presented. The present paper has therefore been written to include in the tables values for this additional stiffness as well as the material of reference I and consequently supersedes reference I.

The method of moment distribution developed by Hardy Cross (reference 2) can frequently be used to advantage in the stress analysis of continuous beams, continuous frames, and rigid joint trusses, some of which occur in aeronautical structures. In reference 3, James summarized the principles of the Cross method and showed how the effects of axial load in the members may be considered in a moment-distribution analysis. In reference 4, it was shown how the principles of moment distribution may be

used to solve problems in the stability of structural members under axial load.

In the stability calculations as well as in the more usual type of moment-distribution analysis in which the effects of axial load are considered, it is desirable to have tables giving the stiffness and the carry-over factor as a function of the axial load and properties of the member. Such a set of tables was presented in reference 1.

In the use of the principles of moment distribution as applied to the stability of plates (reference 5) the stiffness of a plate with the far edge subjected to a moment equal and opposite to the moment applied at the near edge was found useful in stability problems in which the assembly of plates was symmetrical about a plate. Because the equations that must be satisfied for the stability of plates are identical in their general form to those for bars under axial load, a corresponding stiffness for bars is desirable. As is the case for plates, this stiffness is designated SIV, and values are presented herein.

The tables apply to members for which the cross section and axial load do not vary along the length of the member. The interval between successive values of the argument was made sufficiently small that interpolation would be unnecessary for most engineering calculations.

SYMBOLS

- E modulus of elasticity
- E effective modulus of elasticity for stresses beyond the elastic range
- I moment of inertia of cross section about centroidal axis perpendicular to plane of bending
- I length of member
- P axial load in member (absolute value)

$$\alpha = 6 \frac{\frac{L}{j} \csc \frac{L}{j} - 1}{\left(\frac{L}{j}\right)^2}$$

$$\beta = 3 \frac{1 - \frac{L}{j} \cot \frac{L}{j}}{\left(\frac{L}{j}\right)^2}$$

For compression members

$$\alpha = 6 \frac{\frac{L}{j} \operatorname{csch} \frac{L}{j} - 1}{-\left(\frac{L}{j}\right)^{2}}$$

$$\beta = 3 \frac{1 - \frac{L}{j} \coth \frac{L}{j}}{-\left(\frac{L}{j}\right)^2}$$

For tension members

$$j = \sqrt{\frac{EI}{P}}$$

$$\frac{L}{j} = I \sqrt{\frac{P}{EI}}$$

$$\left(\frac{L}{j}\right)_{\text{eff}} = L\sqrt{\frac{P}{EI}}$$

Effective values of α and β are obtained by substitution of $(L/j)_{\mbox{eff}}$ for L/j.

The symbols used to designate the stiffness and carry-over factor for the different types of restraint at the far end are given in the following table and correspond to those used in reference 5:

THE PARTY AND ADDRESS OF THE PARTY AND ADDRESS		
Stiffness	Carry-over factor	Conditions at far end
S	C	Far end fixed against rotation.
s^{I}	c ^I	Far end elastically restrained against rotation.
SII	CII = 0	No restraint against rotation at far end.
s ^{IV}	C _{IV} = -1	Far end subjected to a moment equal and opposite to that applied at near end

The quantities SI, CI, SII, and CII of this paper are the quantities S', C', S", and C", respectively, of references 1 and 4.

DEFINITIONS

The following definitions of carry-over factor and stiffness are the same as those given in reference 4.

Carry-over factor. If a member is on unyielding supports at each end and a moment is applied at the near end, the ratio of the moment developed at the far end to the moment applied at the near end is called the carry-over factor.

Stiffness. - If a member is on unyielding supports at each end, the moment at one end necessary to produce a rotation of one-fourth radian of that end is called the stiffness.

The stiffness of a member computed according to this definition is one-fourth that computed according to the definition used by Cross (reference 2). In the Cross method, the relative stiffness of the members is of importance and not the absolute value. The foregoing definition was selected so that the stiffness of a member of constant cross section with no axial load and fixed at the far end would be $\overline{\text{EI/L}}$ instead of $4\overline{\text{EI/L}}$.

Sign convention. The sign convention used in this report is the same as that used in references 4 and 5. A clockwise moment acting on the end of a member is positive. An external moment applied at a joint is considered to act on the joint; a counterclockwise moment acting on a joint is positive.

TABLES

Tables I and II do not give directly the values of stiffness but give, instead, values of stiffness divided by a factor EI/L. The actual stiffnesses are therefore obtained by multiplying the values in the tables by EI/L. The value of C is read directly from the tables.

Formulas used in calculation. The quantities $\frac{S}{\overline{E}I/L}$, $\frac{SIV}{\overline{E}I/L}$, and C are tabulated for values of $(L/j)_{eff}$ in tables I and II for compression and tension, respectively. The stiffness S^I and carry-over factor C^I that apply when the far end of the member is elastically restrained are dependent on the restraint at the far end and can be computed by the formulas given in reference 4 or 5.

In the elastic range of the material comprising the members, $\overline{E}=E$ and $\left(\frac{L}{j}\right)_{eff}=\left(\frac{L}{j}\right)_{eff}$. Above the elastic range, however, it is necessary to use a reduced modulus \overline{E} which is called the effective modulus. A method for obtaining the effective modulus from the accepted column formula for the material is described in reference μ .

The formulas used in calculating the second, third, fourth, and seventh columns in tables I and II are:

$$C = \frac{\alpha}{2\beta} \tag{1}$$

$$\frac{S^{II}}{EI/L} = \frac{3}{4\beta} \tag{2}$$

$$\frac{S}{\overline{E}I/L} = \frac{S^{II}}{\overline{E}I/L} \left[\frac{1}{1 - C^2} \right]$$
 (3)

$$\frac{S^{\text{IV}}}{\overline{E}\text{J/L}} = \frac{S^{\text{II}}}{\overline{E}\text{J/L}} \left[\frac{1}{1+C} \right] \tag{4}$$

Equations (1) and (2) were first presented by James in reference 3. Equation (3) follows from equation (13) of reference 4, and equation (4), from equation (14) of reference 5.

The fifth and sixth columns in tables I and II were obtained from the preceding columns, as indicated by their headings. These columns are included as a convenience because they are of use in some stability calculations (reference 4).

Accuracy of tables. The tables of reference 6 were used in the preparation of tables I and II. All values presented are accurate to the number of places given. Equations (1), (2), and (3) were used to calculate the second, third, and fourth columns, respectively. The fifth column was obtained by squaring the second column. The sixth column was obtained by squaring the fourth column and multiplying by the fifth column. The sixth column was therefore made to depend on all preceding columns. All values were tabulated to six significant figures and the differences for the last column were taken; in some cases differences as high as the fourth order were used. The differences were studied and, where irregularities occurred, the tables were checked.

An independent check was also made of a series of values throughout the tables. The values for $\frac{S^{IV}}{EI/L}$ were computed from equation (4) and were independently checked.

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Langley Field, Va.

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 Julius Springer (Berlin), 1926.

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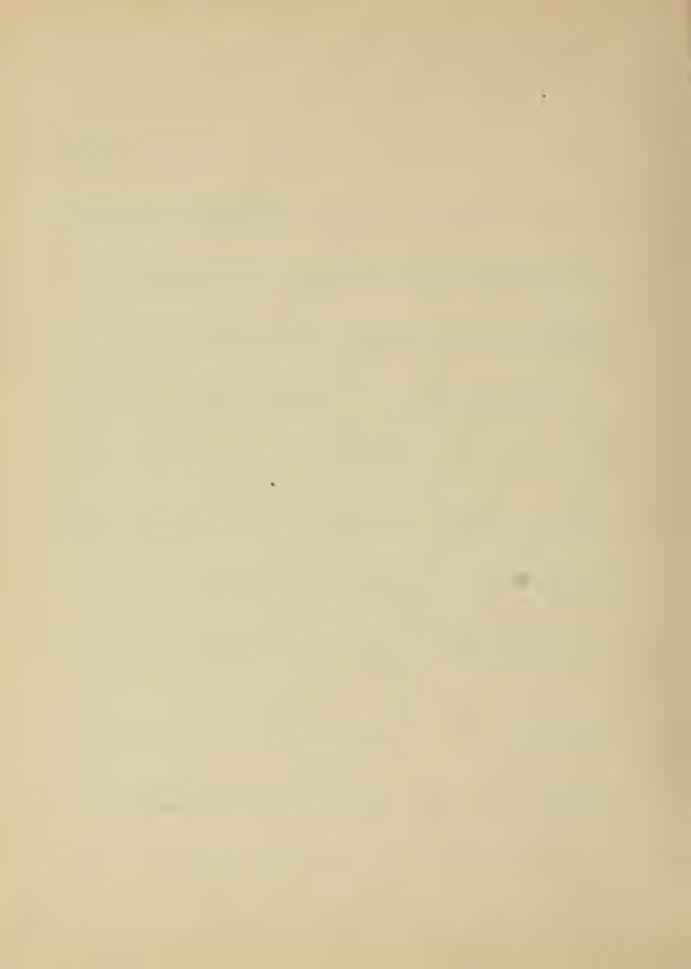
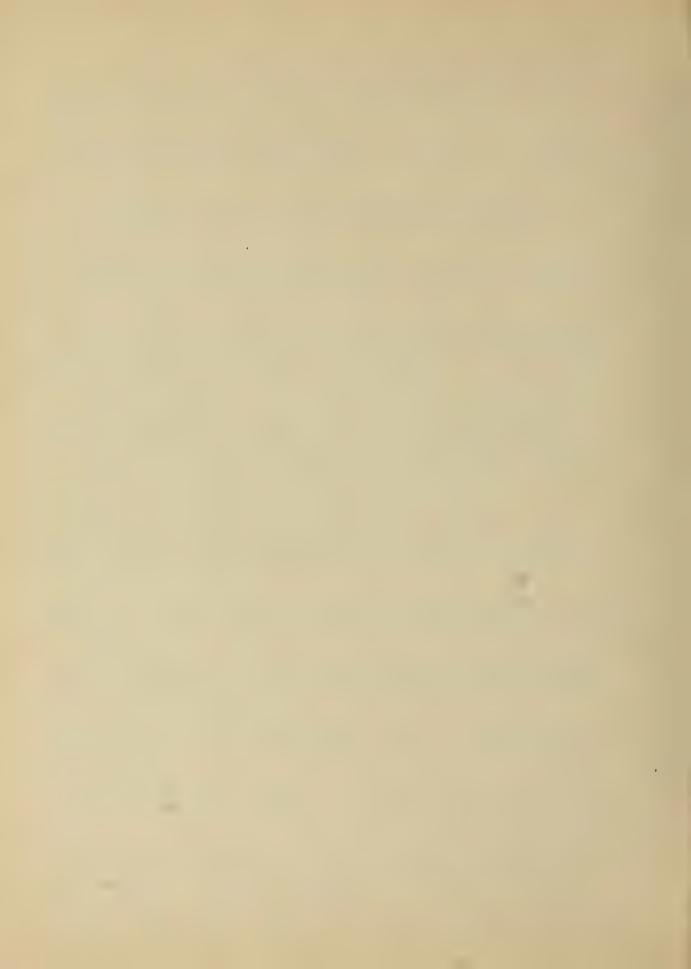


TABLE I -- COMPRESSION - Continued

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TABLE I. - COMPRESSION - Continued

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SII EI/L	-1.96069 -2.02462 -2.09153 -2.16163	-2.51241 -2.59566 -2.47924 -2.56952 -2.66491	-2.76567 -2.98660 -3.10762 -3.25670	-3.57471 -3.52261 -3.68153 -4.05787	-4.23658 -4.45701 -1.69564 -2.95746 -5.24604	-5.56579 -5.92207 -6.32159 -6.772c1 -7.20654	-7.65654 -8.56251 -9.56312 -10.3292 -11.4953	-12.9404 -14.7783 -17.1948 -20.5151 -25.3656	-33.1126 -47.4793 -847.2686 -728.980 -170.947
D	2.90673 2.974.07 3.04469 3.11885 5.19680	3.27885 5.757885 5.75558 5.55504 5.5515	3.6343 7.6743 7.00062 14.13130	1.12004 1.58031 1.75280 1.93895 5.14045	5.59.774 5.59.774 6.14.520 6.14.520	6.81233 7.20372 7.64310 8.13964 8.70595	9.35704 10.1137 11.0040 12.0666 13.3569	14.9567 16.9926 19.6708 23.3522 28.7300	57.3277 53.2714 92.9960 365.751 -189.213
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SIV EI/L	220705 220108 226128 231589	25,12630 25,1829 25,53829 25,53829	276933 276718 268544 268414	500283 506283 512528 518418			- 595199 - 405698 - 415527		- 464878 - 472157 - 479496 - 486894 - 494353
S ² C ² (EI/L) ²	0.458315 1460418 168606 164769 16476997	169231 14173778 1473778 1476091		593080 1493625 1493202 500810 503451	506124 508830 511570 514545 517154	519999 52520.79 525797 528752 571714	.534775 .540956 .540956 .541107 .547299	250 250 250 250 250 250 250 250 250 250	.567361 .570463 .574413 .5746113 .581659
20	2.15031 2.1964.3 2.24416 2.29357 2.34474	2.39776 2.15272 2.50971 2.56683	2.69391 2.76011 2.90049 2.97495	3.0524.7 3.1322 3.521738 3.50514 5.59672	429224 42926 42926 42926 42926 53926	4.04017 4.16581 4.29763 4.13605 4.58151	4.73450 4.09555 5.06524 5.24419 5.45311	5.632.73 6.06.748 6.304.768 6.304.52 6.354.00	6.82343 7.10787 7.41090 7.73418 8.07955
S EI/L	0.161670 157859 157859 150164 150165	244444 244444 2444444 2444444 2444444 2444444	1,1221,65	7,01914 -397723 -393506 -369261 -3649651	.350689 .372063 .367617 .367617	25.02.78 25.12.88 25.12.74 27.12.74 27.12.74 27.27.27 27.27 27.	.336065 .326199 .326799 .322109	.202022 .203022 .298167	288355 2278759 2278705 2278776 312
SII ET/L	-0.531064 -5477798 -564579 -55232	616335 6656934 6655946 6675987	715619 757767 777606 801902	- 524916 - 645432 - 697354 - 922712		-1.09069 -1.12159 -1.15828 -1.22015	-1.25511 -1.28521 -1.5852 -1.40701	-1.4434 -1.49116 -1.59556 -1.58163 -1.62948	1.67922 1.78096 1.94082 1.50053
υ	1.46639 1.46639 1.47805 1.51445	1.5434.7 1.56612 1.50420 1.60276 1.62179	1.66136 1.66136 1.68194 1.70308	1.74713 1.77009 1.79371 1.81801 1.84302	00000000000000000000000000000000000000	2.01002 2.04103 2.07307 2.10619 2.14045	2.17589 2.21259 2.25061 2.25002 2.35090	2.37334 2.46323 2.51068 2.56049	2.66606 2.66606 2.722×0 2.78104 2.94246
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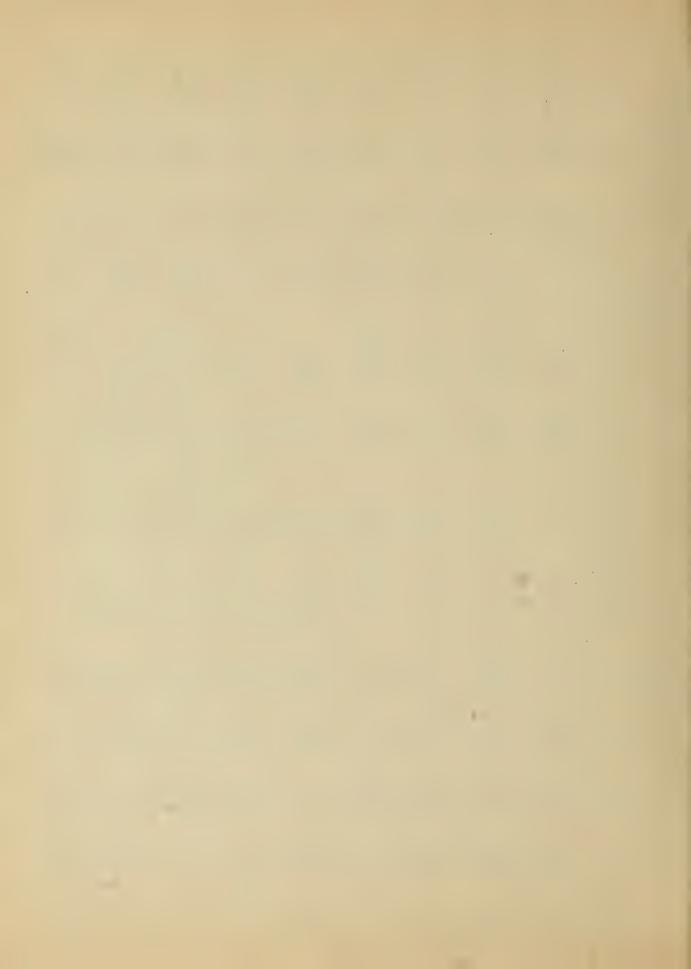
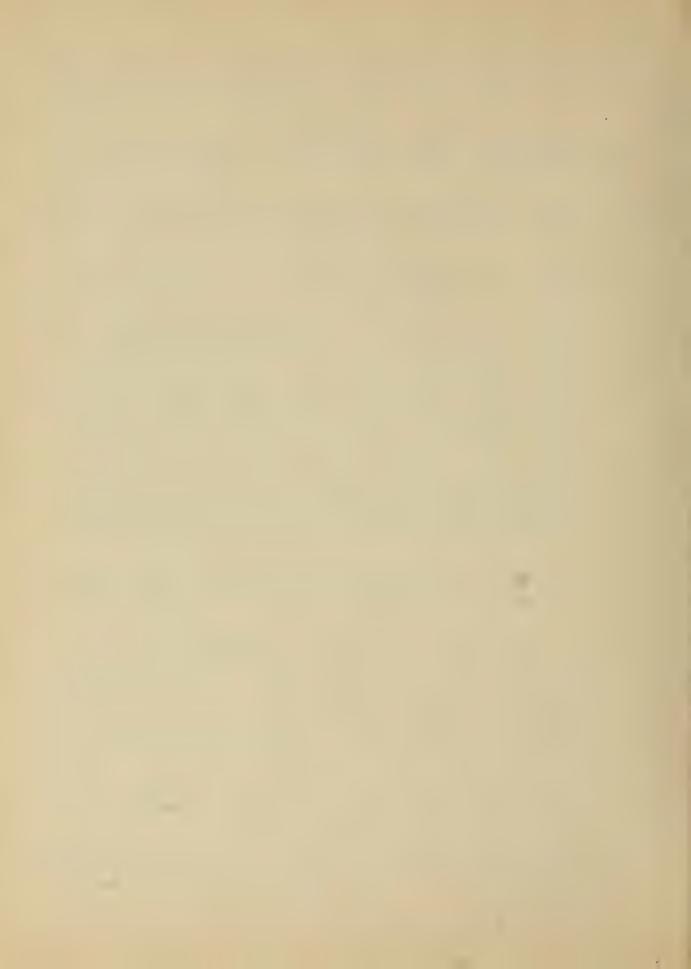


TABLE I.- CONPRESSION - Continued

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\$ ² c ² (EI/L) ²	1.35408 1.37257 1.39150 1.41088	1.45106	11111	1.68469	1.82632 1.85702 1.88659 1.92106 1.95445	2.056881 2.05058 2.05058 2.05807 2.15668	2.17646 2.21746 2.55973 2.30332 2.34828	2.39468 2.14258 2.54311 2.59589	2.65044 2.7665 2.76519 2.82557 2.88807
25	7.36339 7.06763 6.78997 6.52898 6.28335	6.05191 5.62358 5.62741 5.42251 5.24807	5.07337 4.75057 4.660129 4.45939	4.32440 4.19587 5.95665 8.5665	2.73885 5.721 5.5721 5.54004 5.54004 5.5809	3.27286 3.19118 3.03773 2.96561	2.69636 2.76586 2.76586 2.70436 2.64518	22.22 22.23 22.23 22.23 23.23	22.22.7325 22.27.739 22.20100 201000
S EI/L	-0.128829 -140687 -1452697 -161860	-,489661 -,502307 -,515120 -,528106	-554607 -58132 -595732 -595732	-624,161 -658675 -653400 -668344		-779531 -779531 -831065 -831065	866660 985214 922879 942210	961864 981914 -1.00231 -1.02308 -1.0424	-1.06581 -1.08778 -1.11019 -1.15305
SII EI/L	2.72880 2.67393 2.62110 2.57020 2.52111	2.27373	2.25912 2.22011 2.16225 2.14547 2.10973	2.07496 2.04112 2.00817 1.97606 1.94475	1.91420 1.88438 1.85526 1.79698	1.771.76 1.74513 1.71904 1.65349 1.66844	1.64388 1.61978 1.59614 1.57292 1.55011	1.52769	1.42098 1.40062 1.58055 1.56077 1.54126
O	2.71356 -2.65850 -2.6576 -2.55519	2.16006 -2.11528 -2.37222 -2.33077	-2.25241 -2.21534 -2.17958 -2.14506	-2.07952 -2.01838 -2.01827 -1.98913	-1.993561 -1.980715 -1.88150 -1.85663	-1.80910 -1.78639 -1.76433 -1.74291	-1.70187 -1.66321 -1.66509 -1.64449	-1.60880 -1.59166 -1.574°8 -1.55875 -1.54291	-1.52750 -1.51248 -1.49784 -1.48556
$\left(\frac{1}{3}\right)$ eff	200000000000000000000000000000000000000	00000 00000 00000	27.7.7. 000.01 000.00	2255 1241 1274 1274 1274 1274 1274 1274 1274		200000 100000 100000	2445 2445 2446 2446 2446 2446 2446 2446	で で で で で で で で で で で か で か か か か か か か	
SIV EI/L	-0.919632 -942725 -954453	978285 990593 -1.00263 -1.01500	-1.04015 -1.05293 -1.06586 -1.07892	-1.10551 -1.11903 -1.14654 -1.16055	-1.17469 -1.20351 -1.21818 -1.23302	-1.24805 -1.26326 -1.27866 -1.29424 -1.31002	-1.32600 -1.35857 -1.35857 -1.39199	-1.40902 -1.42628 -1.4576 -1.46148 -1.47944	-1.5764 -1.53479 -1.53479 -1.55375 -1.57298
$\frac{s^2c^2}{(\overline{E}I/L)^2}$	0.825660 831158 831158 838787 844551	.862495 .870682 .879016 .867502 .896143	904945	951169	1.00261 1.01345 1.02450 1.03577 1.04727	1.05900	1.12464 1.13464 1.14519 1.16203	1.20526 1.20576 1.22047 1.23589	1.26777 1.28426 1.30112 1.31837 1.33602
20	5649.83 2199.51 1161.65 716.577 485.765	350.878 265.283 207.590 166.871 137.064	114.593 97.2340 83.5462 72.5630 63.6161	56.2316 50.0659 144.8647 140.1270 56.2367	25.3506 27.9844 25.7775 25.8237	22.0857 20.5529 19.1598 17.6853 16.7516	15.7237 14.7689 15.9362 13.1563	11.7839 11.1782 10.6191 10.1018 9.62219	8.76244 8.76244 8.37628 8.01583 7.67686
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S EI/I	-0.0120741 -0194392 -0268713 -0543712 -0419402	- 0495793 - 0572895 - 0650721 - 0729281		-158567 -1147141 -155801 -164549		2216974 227694 257694 257627	267053 2287035 2297196	2317865 2329379 2329377 2329377 2329377	371685 382837 594124 405550
I ST H	010000000000000000000000000000000000000	049579 057289 065072 072928 030858	088865 096948 105110 115352 121674		173786 162315 191336 200452 209664	216974 2276974 2277594 2577507	267053 276988 287035 297196	317865 328379 359015 360666	571685 582837 594124 405550 417117
	8.2048 -0.012 2.7273 -0.019 1.1882 -026 4.5953 -034	7.3467 - 049579 5.1406 - 057289 5.04433 - 065072 2.0966 - 072928	0.0945088865 52975096948 07647105110 113552 121674	15447 145429 145429 145431 186397	60914173566 37645162315 16309191336 96671209664	.61722 - 228363 .46097 - 228365 .31534 - 277694 .17924 - 247507	.81937267053 .81937276988 .71315287035 .61280297196	.42781317865 328379 26102359015 1858349777 10973360666	.03919371685 -97175382837 -90717394124 .84527405550



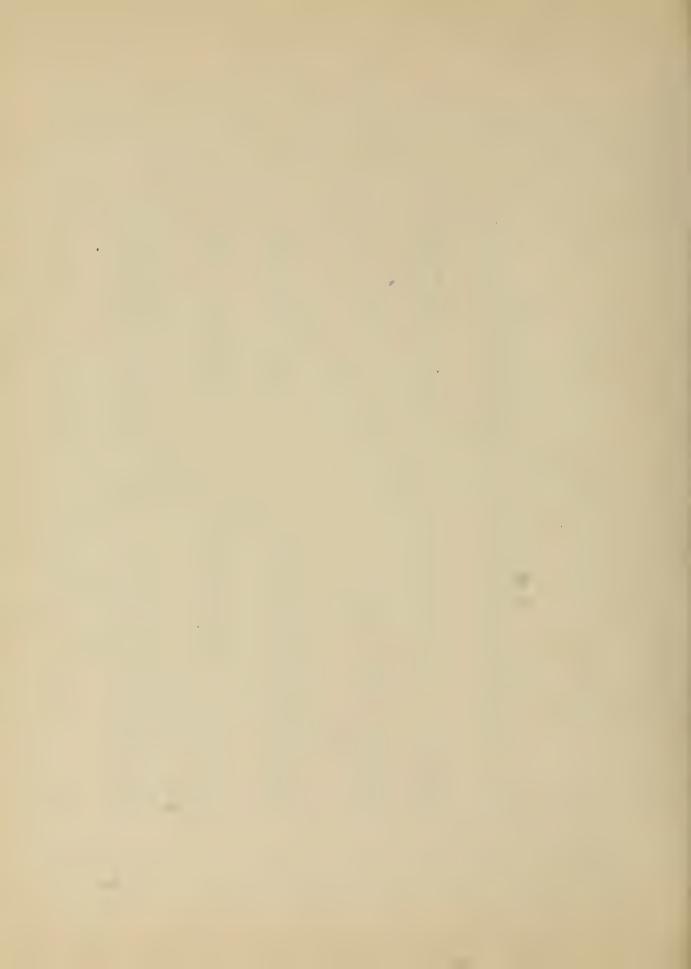
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	S IV	-6.8200h -7.0200 -7.19289 -7.55356 -7.55356	826 060 060 369 369		-10.9314 -11.5707 -11.5446 -12.3573	and or the	-17.5960 -18.7101 -19.9695 -21.4041	450WC	するうろう	-134.993 -237.76 -985.9
	\$2 c ² (\overline{\mathbb{E}}1/\mathbb{L})^2	12.26495	WWW. 120	25.57	70110	· 017/20	78.5430 100.844 115.688	10001-+	-+W	4557.02 14133.6 242990
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OMPRESSION -	S II/I	2.7.7.8.6 5.7.7.7.8.6 5.7.7.7.8.6 5.7.7.7.8.6 5.7.7.7.8.6 5.7.7.8.6 5.7.7.8.6 5.7.7.8.6 5.7.8.				7801 8501 8501	-01 Ct • •	5.570 5.570 5.570 5.559 5.559	-21.1757 -24.5774 -29.2570 -36.1011	-67.4876 -118.075 -492.94
ABLE I CO	SII EI/L	0.612739 0.598672 5598672 570587 556562	54.2546 528535 514527 500518	172491 172491 1720312 1730312	7, 1022 34 7, 1022 34	7227	5978 5978 5979 5079 1622 0160	186914 172166 157353 142472 127521	112495 0973934 06622118 0669474 0515970	0361576 000000000000000000000000000000000000
H	υ	-1.08984 -1.08550 -1.08128 -1.07718		- AAAAA		9999	00000	2000	-1.00265 -1.00140 -1.00040 -1.00093	-1.00027
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		95278 001983 008931 16136 -3.0	33.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.	3.74894 -3.3838 3.94673 -3.4591 5.94854 -3.4958 4.05461 -3.5540	4.528047 1.52641 1.52641 1.52641 1.79489	1755 1755 1755 1755	2527	.82554 -4.843 .07290 -4.943 .23415 -5.045 .90253 -5.153	221206 221206 225909 25909 25909	
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SSION - Continued	$\frac{s^2c^2}{(\overline{E}_1/L)^2} \frac{s^4}{\overline{E}_1/L}$	2.12025 2.95278 -2.9 2.08192 3.01983 -2.9 2.04487 3.08931 -2.9 2.0905 3.16136 -3.0	94090 3.31363 -5.1 90848 5.39414 -3.1 84771 5.4775 -3.1 84674 3.56465 -5.2 841733 5.55498 -5.3	78886 5.74894 -5.3838 .76128 5.34675 -5.4591 .73456 5.94874 -3.4958 .70867 4.05461 -5.5540	65926 4.28047 -3.6 65568 1.440079 -3.7 601282 4.52641 -3.8 7.99065 4.65767 -3.8	1.54830 4.93843 -4.008 1.52807 5.08870 -4.080 1.50845 5.4609 -4.155 1.48941 5.41108 -4.232 1.47093 5.58416 -4.311	1,5501 5.76585 -4.393 1,5561 5.95674 -4.177 1,1273 6.36864 -4.564 3,20645 6.59107 -4.747	23124 1.37102 6.82554 -4.843 28362 1.35604 7.07290 -4.943 7.35018 1.34151 7.35415 -5.046 7.35411 1.32741 7.51031 -5.153 4.5263 1.31372 7.90253 -5.263	51293 1.30044 6.21206 5.57545 1.28756 8.54029 5.5706 5.70766 5.70766 5.70766 5.70765 1.25117 9.65319 5.70765	22976 10.0721 -6.2729 10.5211 -6.2729 11.5119 -6.20759 12.0606 -6.20759 12.0606
BLE I COMPRESSION - Continued	$\frac{s}{1/L}$ $c^2 \frac{s^2 c^2}{(E_I/L)^2} \frac{s^{\Gamma}}{E_I}$	-1.18011 2.12025 2.95278 -2.8 -1.20437 2.08192 3.01983 -2.9 -1.25442 2.06487 3.08931 -2.9 -1.25642 1.97441 3.25609 -3.0	.30662 1.94090 3.31363 -3.1 .33558 1.90848 3.59414 -3.1 .36115 1.8771 3.47775 -3.2 .36933 1.84674 3.56465 -3.2 .151516 1.41733 3.65498 -3.3	1.44766 1.78886 3.74894 -3.3838 1.47785 1.76128 3.84677 -3.45391 1.50877 1.73456 3.94854 -3.4458 1.14044 1.70867 4.05461 -3.5540 1.57289 1.68358 4.16516 -3.6137	1.60616 1.65926 4.28047 -3.6 1.64027 1.63568 1.140079 -3.7 1.67527 1.61282 1.52641 -3.8 1.71119 1.59065 1.65767 -3.8 1.74506 1.56915 1.79489 -3.9	1.78594 1.54830 4.93843 -4.008 1.82863 1.52807 5.08870 -4.080 1.90605 1.48941 5.41108 -4.232 1.94542 1.47093 5.58416 -4.311	99204 1.45301 5.76585 -4.393 03697 1.43561 5.95674 -4.477 005329 1.41873 6.15744 -4.564 1.13106 1.416.25 6.36864 -4.564 1.18035 1.30645 6.59107 -4.747	11 -2.23124 1.37102 6.82554 -4.843 -2.28362 1.35604 7.07290 -4.943 1.34151 7.23415 -5.046 -2.39441 1.32741 7.51031 -5.046 -2.39441 1.32741 7.90253 -5.153	2.51292 1.30044 8.21206 -5. 2.57545 1.28756 8.54029 -5. 2.70765 1.26293 9.65319 -5.	2.05045 1.22976 10.0751 -6.075251 2.05052 1.22870 10.5211 -6.050719 11.2199 11.5119 -6.0517554 11.9752 11.5119 -6.0506 11.5119
I COMPRESSION - Continued	$\frac{1}{\sqrt{L}}$ $\frac{s}{E_{\rm I}/L}$ $\frac{s}{(E_{\rm I}/L)^2}$ $\frac{s^2 c^2}{s_{\rm I}}$ $\frac{s}{E_{\rm I}}$	1.36202 -1.18011 2.12025 2.95276 -2.8 1.36428 -1.20437 2.08192 5.01963 -2.9 1.28428 -1.25442 2.0905 5.08931 -2.9 1.26577 -1.25442 2.0905 5.16136 -3.0	.22940	.12506 -1.44766 1.78866 5.74894 -5.3838 .12506 -1.47785 1.76128 5.94675 -5.4591 .10528 -1.50877 1.774,56 5.94854 -5.4591 .03166 -1.54044 1.70867 4.05461 -5.5450 .07519 1.57289 1.68358 4.16516 -3.6137	.05887 -1.60616 1.65926 4.28047 -3.6 .01269 -1.64027 1.65568 4.140079 -3.7 .02664 -1.67527 1.61262 4.52641 -3.8 .01071 -1.7119 1.59065 4.65767 -3.8 994913 -1.74506 1.55915 4.79489 -3.9	979230 -1.78594 1.54830 4.93843 -4.008 962660 -1.82487 1.52807 5.08870 -4.080 948198 -1.86489 1.50845 5.24609 -4.155 32888 -1.90605 1.48941 5.41108 -4.232 917577 -1.94842 1.47093 5.58416 -4.311	8922410 -1,99204 1,45301 5,76585 -4,393 887233 -2,0329 1,41873 6,15744 -4,564 877237 -2,13106 1,16235 6,36864 -4,564 842593 -2,18035 1,35645 6,59107 -4,747	.17090 .827831 -2.23124 1.37102 6.82554 -4.843 .15419 .513139 -2.28352 1.35604 7.07290 -4.943 .15324 .728512 -2.33016 1.34151 7.33415 -5.046 .15213 .785947 -2.33016 1.3172 7.90253 -5.263	14.037 -754987 -2.51293 1.30044 6.21206 -5. 13471 -740586 -2.57545 1.28756 8.54029 -5. 12918 -76233 -2.64031 1.28756 8.54029 -5. 12938 -71324 -2.70766 1.26293 9.25909 -5.	683427 -2.95625 1.22870 10.0731 -6.65925 2.95627 1.22870 10.9938 -6.65936 -5.06755 1.20759 11.5119 -6.65625 1.20759 11.5119 -6.65625 1.20759 11.5119 -6.65625 1.20759 11.5119 -6.65625 1.20759 11.5119 -6.65625 1.20759 11.5119 -6.65625 11.5119 -6.



TABLE II.- TENSION

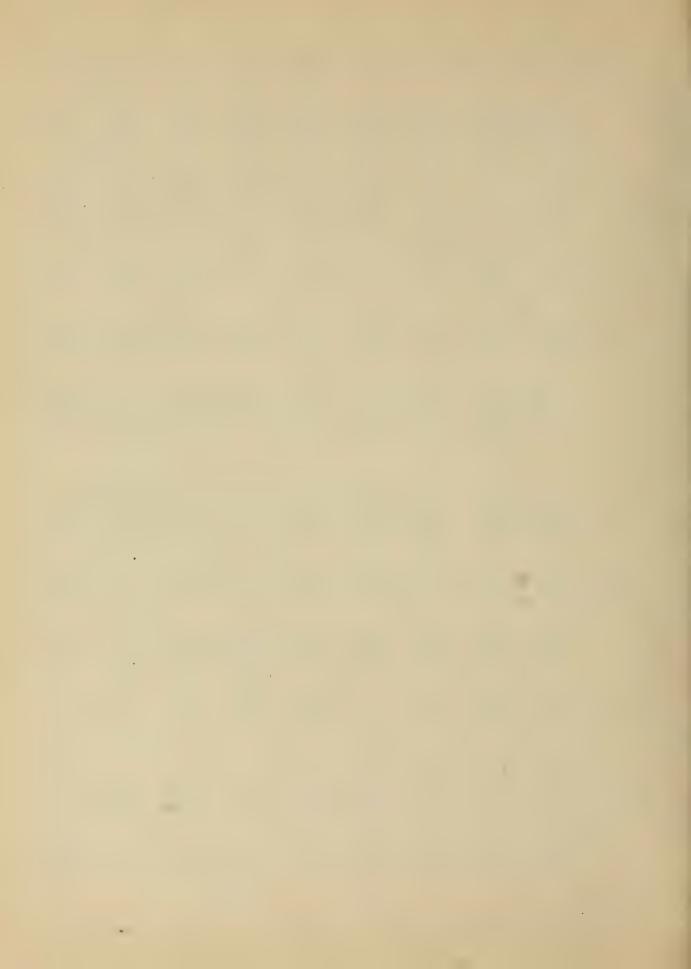
$\left(\frac{L}{J}\right)_{eff}$	С	SII EI/L	S ĒI/L	c ²	S ² C ²	SIV EI/L
0 1 2 3 4 5	0.500000	0.750000	1.00000	0.250000	0.250000	0.500000
	.499757	.750512	1.00036	.249757	.249936	.500422
	.499001	.751996	1.00133	.249002	.249665	.501666
	.497760	.754488	1.00300	.247765	.249252	.503744
	.496033	.757964	1.00532	.246049	.248675	.506649
	.493831	.762412	1.00831	.243869	.247937	.510374
.6 .7 .8 .9	.491167 .488057 .484519 .480575 .476246	.767818 .774165 .781431 .789595 .798632	1.01194 1.01623 1.02116 1.02672 1.03291	.241245 .238200 .234759 .230953 .226810	.247042 .245994 .244798 .243459 .241983	.514911 .520252 .526386 .533303 .540988
1.1	.471556	.808515	1.03971	.222365	.240376	.549428
1.2	.466530	.819215	1.04712	.217651	.238646	.558608
1.3	.461194	.830703	1.05513	.212700	.236799	.568510
1.4	.455575	.842949	1.06372	.207548	.234843	.579118
1.5	.449699	.855921	1.07289	.202229	.232785	.590413
1.6	.443594	.869586	1.08262	.196775	.230633	.602376
1.7	.437286	.683915	1.09290	.191219	.228396	.614989
1.8	.430802	.898873	1.10371	.185590	.226081	.628230
1.9	.424167	.914429	1.11505	.179918	.223697	.642080
2.0	.417408	.930553	1.12689	.174229	.221251	.656518
2.1	.410548	.947214	1.13923	.160550	.218751	.671522
2.2	.403610	.964380	1.15205	.162901	.216205	.687071
2.3	.396616	.982024	1.16534	.157305	.213621	.703145
2.4	.389588	1.00012	1.17908	.151779	.211006	.719723
2.5	.382544	1.01863	1.19325	.146340	.208366	.736702
2.6 ·	.375502	1.03754	1.20785	.11,1002	.205709	.754303
2.7	.368480	1.05683	1.22287	.135777	.203042	.772264
2.8	.361492	1.07646	1.23827	.130677	.200369	.790646
2.9	.354553	1.09642	1.25406	.125708	.197697	.809429
3.0	.347676	1.11668	1.27022	.120878	.195032	.828594
3.1	.340871	1.13722	1.28673	.116193	.192378	.848120
3.2	.334149	1.15803	1.30358	.111656	.189740	.867991
3.3	.327520	1.17909	1.32076	.107269	.187122	.868188
3.4	.320990	1.20037	1.33826	.103034	.184529	.908693
3.5	.314566	1.22188	1.35606	.0989519	.181963	.929491
3.6 3.7 3.8 3.9 4.0	.308255 .302062 .295990 .290042 .284221	1.24358 1.26547 1.25754 1.30976	1.37416 1.39253 1.41117 1.43007 1.44921	.0950214 .0912413 .0876098 .0841242 .0807615	.179429 .176929 .174466 .172042 .169658	.950564 .971898 .993477 1.01529 1.03731
4.1	.278529	1.35466	1.46859	.0775783	.167318	1.05955
4.2	.272967	1.37731	1.43820	.0745108	.165022	1.08197
4.3	.267535	1.40009	1.50802	.0715749	.162771	1.10457
4.4	.262234	1.42297	1.52605	.0687666	.160566	1.12735
4.5	.257063	1.44597	1.54828	.0660815	.158409	1.15028
4.6	.252022	1.46907	1.56870	.0635151	.156300	1.17335
4.7	.21.7110	1.49225	1.58930	.0610631	.154238	1.19657
4.8	.21.2321	1.51553	1.61008	.0587210	.152225	1.21992
4.9	.237661	1.53889	1.63101	.0564843	.150260	1.24338
5.0	.233128	1.56232	1.65211	.0543466	.14c343	1.26696



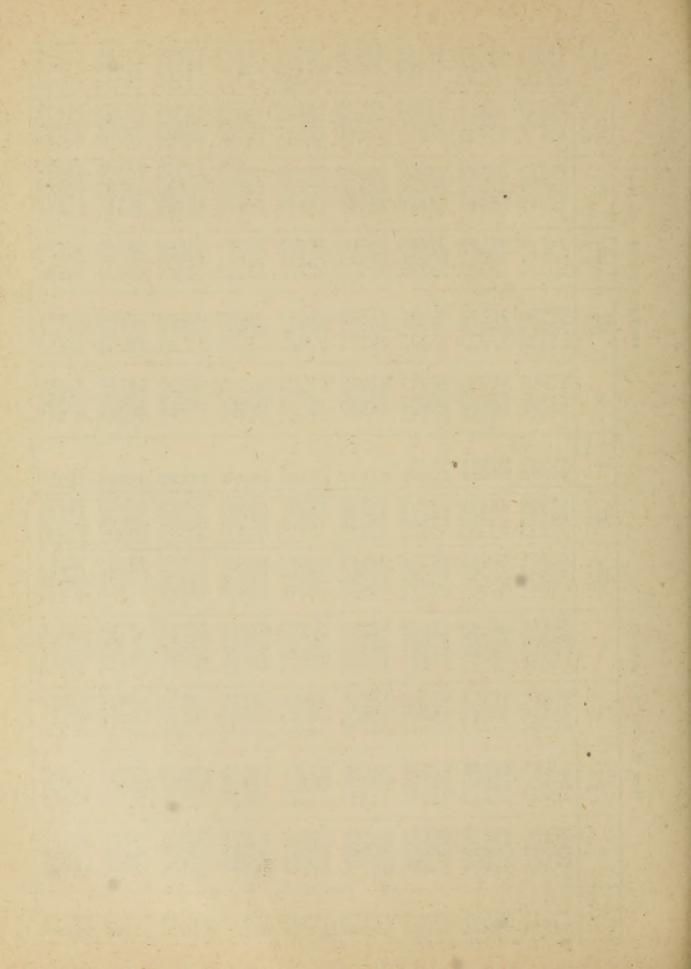
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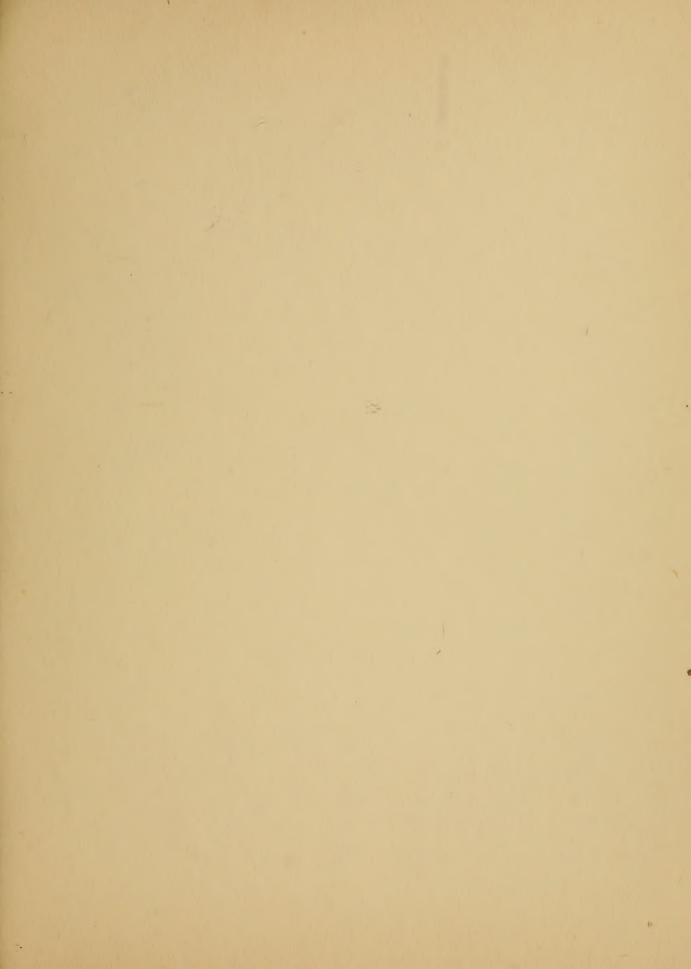
TABLE II.- TENSION - Continued

									15
SIV EI/L	2.10033 2.12530 2.15527 2.17525 2.50033	2.52521 2.55019 2.57517 2.60016 2.62514	2.65013 2.67512 2.72510 2.72510	2.477508 2.885500 2.885500 2.885500 2.885500	2.90005	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3.15002 3.17502 3.225002 5.22502 5.25502	3.27501 3.25501 3.75501 3.75501	24,2501 24,2501 24,5001 25,0001
\$ ² C ² (EI/L) ²	0.0994567 .098421 .098421 .0974515 .0974746	.0970094 .0961150 .0961150 .0956810	.09454.75 .0940527 .0956691 .0956691	0929279 0925698 0922196 0915773	0912148 0908943 090506 0905736 0905736	0896787 0891081 0881081 0888104 08883605	2682947 0230342 0877789 0875285 0875285	0870421 0665739 0665739 0861230	000000000000000000000000000000000000000
250	0.0154857 .0154864 .01258852 .0125996	.0120558 .0117968 .0115460 .0115030	.0106392 .0106179 .0104032 .0101945 .0101945	009 20 638 000 79 658 000 20 600 000 20 600 000 20 600	.00689618 .00673100 .00857035 .00841408	.00811404 .0070298 .00702971 .00702971	.0072057 .00730400. .00716085 .00716087	.00682940 .00671797 .00650923 .00650311	.00629839 .00615963 .00610317 .00600895 .00591688
S EI/L	2.71569 2.73985 2.76402 2.78622 2.81244	2.85667 2.86092 2.88519 2.90948 2.95379	2.95611 2.98244 7.00679 7.03115 5.05553	3.07992 3.12673 5.12675 5.175818	3.20207 5.22654 5.25101 5.27550 5.29999	3.32450 5.345901 5.375901 5.39807 5.42261	3-14717 5-14717 5-149629 5-52087 5-54545	3.57004 3.594.64 3.61925 5.61925 5.64366	3.69310 3.71773 3.74237 3.76702
SII EI/L	2.67907 2.72841 2.75509 2.75509	2.80247 2.82717 2.85188 2.87660 2.90132	2.92604 2.97551 2.00025 3.02500	3.04975 3.097451 3.09927 3.12494 3.14881	3.117358 3.127358 3.22315 3.247794 3.2773	2000 2000 2000 2000 2000 2000 2000 200	3,42155 3,44637 3,49601 3,52083	25,54566 25,55704566 25,557349 26,550166 26,550166	5.66984 5.71953 7.71953 7.71953 7.71953 7.71953
D	0.116128 114806 113513 112248	109799 108613 107452 106316	.104112 .105043 .109969 .100969 .109999633	.0989767 .0980092 .0970602 .0961293	.0943196 .0934398 .0925762 .0917283	0900080 0880 0881840 0881840 0801840 0801840	08546396 0854635 0847398 0847398 0847398	.0826402 .0819652 .0812972 .0806419	.0753624 .0757373 .0751228 .077517
$\left(\frac{L}{J}\right)_{\text{eff}}$	9.6 9.9 10.0	1001	10.9	111111	11.6	122 122 123 123 123 123 123 123 123 123	12.0 12.9 12.9 13.9	1000 1000 1000 1000 1000 1000 1000 100	11111
SIV EI/L	1.29064 1.31442 1.35829 1.36225 1.386225	1.45457 1.45881 1.45881 1.50745	1.55186 1.55630 1.60533 1.62089	1.65450 1.67913 1.70379 1.72848	1.87793 1.80269 1.85247 1.85226	1.90190 1.92674 1.97647 2.00134	2.02623 2.05113 2.07603 2.10094 2.12587	2.15079 2.20066 2.22561 2.25561	2.27551 2.32543 2.355039 2.37536
\$2c2 (\overline{	0.146475 114654 112880 112880 1139472	.157836 .156245 .151696 .151751	.130310 .125930 .125930 .126285	.123791 .122597 .120512 .120512	.113157 .115125 .115124 .115251	112269 112398 111532 110690	200.001. 100.505. 100.501. 100.1.	105423	102241 101654 101005 100527 0099040
ر ₂	0.0523097 0.0583097 0.0485054 0.0467319 0.0450388	0454225 0418794 0404059 0589987 0589987	.03563706 .0351437 .0358710 .0326499	.0297715 .0297715 .0288326 .0279338	.0262484 .0254582 .02547007 .0259745 .0252775	.0226089 .02195671 .0213507 .0207586	.0196427 .0191167 .0186107 .0181238	.0172035 .0167656 .0163455 .0159454	0151797 0145169 0144666 0141285 0155015
S I/I	1.67536	1.80368 1.80368 1.82582 1.84806	1.89284 1.91537 1.95069 1.96069	2.02927 2.02927 2.05227 2.05227 2.09847	2.12167 2.14493 2.16824 2.19160 2.21502	2.23619 2.26200 2.28516 2.30917 2.35281	2.35650 2.35650 2.450399 2.45162	2.47548 2.52938 2.52931 2.54726	2.59526 2.61336 2.641336 2.66745 2.66745
SII EI/L	1.58583 1.69940 1.65304 1.65674	1.72814 1.75204 1.7599	1.82400 1.84506 1.87215 1.59628	1.94463 1.96885 1.99310 2.01737 2.04166	2.06598 2.09032 2.11468 2.13906 2.16346	2.18788 2.218731 2.23676 2.26123,	2.351021 2.35925 2.35925 2.36378 2.40833	2.45289 2.45747 2.50665 2.50665	2.55586 2.58049 2.60512 2.62976 2.65441
o o	0.228713 2204418 220259 216176	.208381 .201645 .201012 .197481	.190711 .187466 .184512 .151245	175364 172544 169802 167134 161539	.159556 .159556 .157164 .154836	150363 118213 114079 142090	158263	.131162 .129494 .127865 .126275 .126275	.123206 .12724 .120277 .118862 .117480
$\left(\frac{L}{J}\right)_{\text{eff}}$	กกกกก พูตั้งจุ๋ก	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	00000 40040	92.000	 	21.00 0.00 0.00 0.00	ಹಹಹಹಾದ ಇಗೆ ಬ್ ಕೆಸ್	0000000 000000	00000 10070



	SIV EI/L	1.65000 1.67500 1.72500 1.72500	4.77500 4.62500 4.85000	1.90000 1.92500 14.95000 5.00000	5.25000 5.75000 6.00000 6.25000	6.50000 6.75000 7.25000 7.50000	7.75000 8.50000 8.75000	99.55000	10.2500	11.5000 11.7500 12.2500 12.5000
TABLE 11 IFNSION - Continued	S ² C ² (EI/L) ²	0.0784674 0783664 0782667 0781652 0781652	.0779748 .077879 .0777861 .0776935	0775116 0775223 0775340 0775467 0772467	0763504 0756250 0749716 0749302 0738422	0733507 0729000 0724852 0724852 0721022	.0714180 .0711111 .0705247 .0705566	0700692 0699469 0694394 0694394	06907463 0687463 0687463 0685941	.0683110 .0681790 .0689529 .0679323 .0678168
	°2°	0.00522830 .00519195 .00515617 .00512130 .00508642	.00\$05241 .00501896 .00508605 .00598605 .00595605	.00289051 .00285968 .00282933 .00279947	.00250000 .00226757 .00206612 .00189036	.00160000 .00147929 .00177174 .00127511 .0012906	.00111111 .00104.058 .000976563 .000918274 .000865052	.000816326 .000771605 .000750460 .00069251	.000625000 .000594884 .000566893 .00056893	000493827 000472594 000452694 000434028
	S EI/L	4.93012 4.95494 4.97976 5.00459 5.02941	5.05424 5.07907 5.10390 5.12874	5.17841 5.20325 5.22609 5.25290 5.27778	5.52632 5.77500 6.02381 6.27273 6.52174	6.77083 7.02000 7.26923 7.51852	8.01724 8.26667 8.51613 8.76563 9.01515	9.51429 9.51429 9.76389 10.0135	10.5128 10.7625 11.0122 11.2619 11.5116	11.7644 12.0111 12.2609 12.5106 12.7604
	SII EI/L	4.91420 4.95912 4.96405 1.96897 5.01389	5.05381 5.06374 5.08866 5.11259 5.112551	5.16344 5.18337 5.21330 5.23823 5.26316	5.51250 5.76190 6.26087 6.51042	6.76000 7.00962 7.50893 7.75862	8.00833 8.25806 8.50781 6.75758	9.25714 9.50694 9.756 76 10.0066	10.5063 10.7561 11.0060 11.2558 11.5057	11.7556 12.0054 12.2553 12.5052 12.7551
	O	0.0568182 0561972 0561798 0558659	.0552486 .0549450 .0549458 .0543478 .0543478	.0527634 .0534759 .0531915 .0529100	0500000	. 04,00000 . 05,84615 . 05,727 . 05,7145 . 05,7145	.0353533 .0352581 .0312500 .0305030	.0285714 .0277778 .0277279 .0263158	.0250000 .0245902 .0258095 .0252558	.0222222 .0217391 .0217391 .0208373
	JJe't	18.6 18.9 19.9	19999	20.05	22 23 25 25 25 25 25	226 229 30	TAKAS.	69876	132 <u>1</u> 2	0 2 4 4 5 6 4 4 5 6 4 4 5 6 6 4 6 6 4 6 6 6 4 6 6 6 6
	SIV EI/L	3.52501 3.55000 3.57500 3.60000	3.65000 3.67500 3.72500	23.82500 3.82500 3.85500 3.85500	3.92500 3.92500 5.97500 4.00000	4.02500 4.05000 4.07500 4.12500	4.15000 4.17500 4.22500 4.25000	4.27500 4.32500 4.35500 4.37500	1, 1,0000 1, 1,2500 1, 1,5000 1, 1,7500	4.52500 4.57500 4.57500 4.60000 4.62500
	s ² c ² (EI/L) ²	0.0548651 0.08446681 0.0844746 0.0842845	00833913 0083357333 0083357333 008335033 008335033	.08267294 .0827091 .0827091 .0825480	0820794 0819260 0819260 0817769	0814874 0813450 0812646 0812646	0807258 0805350 0805350 0804043	0301525 0800292 0799077 0797878	.0795528 .0794377 .0793241 .0791015	0789923 0788784 0786735 0786735 0786735
	20	0.00582692 .00573899 .00568899 .00556899	.00540643 .00532780 .00525088 .00517561	.00502984 .00495928 .00489015 .0048247	000469126	000132823	200410912 004050400 46950400 55556500 45906500	.00585787 .00581059 .00576378 .00571802	.00562897 .00558564 .005585027 .00550127	.00341985 .00338020 .00334124 .00330294 .00326530
	S EI/L	3.81632 3.81698 3.86565 3.91500	2.92968 2.98457 2.98906 4.01376 4.01376	4.06517 4.08788 4.11259 4.13731 4.13731	4.218676 4.23623 4.26097 4.28971	4.33521 4.33521 4.35596 4.35596 4.356472	11.50878 11.50856 11.50856	4.558811 4.56889 4.65247 4.65247	4.68205 4.775685 4.775645 4.78645	14.80606 14.85086 14.85567 14.88567 14.90550
	SII EI/L	3.794.08 3.84.3804 5.86.866 5.89.352	3.91838 3.94325 3.96812 7.9299 4.01786	11.04273 11.06761 11.09248 11.11736	4.16712 4.19201 4.21689 4.24178 4.2667	4.29156 4.34134 4.3623 4.36623	14.11603 14.146582 14.19672 14.51562	1.55557 1.55557 1.59034 1.61524 1.64015	4.66506 4.71488 4.73979 4.75979	4.78962 4.81453 4.85945 4.86437 4.88929
	O	0.0763343 .0757561 .0751866 .0746257	.075528h .0729918 .0724630 .0719117	0709214 0704220 0699296 0694440	0684928 0684928 0686269 0675673 067138	0657893 0657893 0657893 0657893 06593593 06593593	.0652910 .0652910 .0652900 .0628950		.0598802 .0598802 .0595238 .0591716	.0584795 .0581395 .0578034 .0574712 .0574718
	$\left(\frac{L}{3}\right)$	44444 10.040	5.500 ₹₹₹₹₹ \$000 \$000 \$000 \$000 \$000 \$000	15.21	15.6	16.5	16.9	17.2	17.6	198.3221







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